# The Effect on Metal-Metal Bonds of Increased Concentration of Hydrogen in Hafnium Dihydride 

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#### Abstract

A tetragonal unit cell of hafnium dihydride is formed at a composition of $\mathrm{HfH}_{1.87}$. Each metal atom has 12 Hf atoms as its neighbors, 8 at a distance $3.289 \pm 0.002 \AA$ and 4 at $3.461 \pm 0.002 \AA$; they constitute short and long metal-metal bonds respectively. As the concentration of hydrogen atoms is increased, the dihydride structure exhibits anisotropic changes; $a_{0}$ increases and $c_{0}$ decreases. It is shown that the anisotropy arises from the additional metal-gas bonding, which strengthens the short and weakens the long metal-metal bonds.


## Introduction

Hafnium dihydrides formed in the composition range of $\mathrm{HfH}_{1.87-2.10}$ crystallize in a deformed fluorite-type tetragonal structure contracted along the $c$ axis. As the concentration of hydrogen increases, the symmetry of the face-centered tetragonal unit cell remains the same but its lattice parameters change; $a_{0}$ increases and $c_{0}$ decreases. The volume of the unit cell also increases. This paper presents experimental evidence of these changes and their relation to metal-metal bonds in the dihydride.

## Experimental procedure

The samples were prepared by heating and outgassing the metal in an evacuated quartz tube at $1100^{\circ} \mathrm{C}$. The temperature was then lowered to $1000^{\circ} \mathrm{C}$. and a measured volume of purified gas was admitted into the tube at a known pressure. The volume of gas was in excess of the theoretical absorption for the dihydride. Most of the absorption of gas took place at $700-800^{\circ} \mathrm{C}$. The sample $\mathrm{HfH}_{1.98}$ was cooled from $750^{\circ}$ to $350^{\circ} \mathrm{C}$. at a rate of $2.5^{\circ} \mathrm{C}$. per min., annealed at $350^{\circ} \mathrm{C}$. for 24 hr . at a decomposition pressure of the dihydride, and then cooled to room temperature in the furnace in $1 \frac{1}{2} \mathrm{hr}$.

The sample $\mathrm{HfH}_{2.10}$ was cooled from $750^{\circ}$ to $350^{\circ} \mathrm{C}$. at a slow rate of about $0 \cdot 4^{\circ} \mathrm{C}$. per min., annealed at $350^{\circ} \mathrm{C}$. for 48 hr ., cooled further to $225^{\circ} \mathrm{C}$. at the above rate and then cooled in the furnace in $1 \frac{1}{2} \mathrm{hr}$. The gas pressure in the tube during cooling from $350^{\circ} \mathrm{C}$. to room temperature varied from 170 to 150 mm . The hafnium deuteride sample was prepared the same way as $\mathrm{HfH}_{2.10}$. The deuterium gas used was $99.5 \%$ pure and was obtained from Stuart Oxygen Company. Compositions of the samples were calculated from the weight of the metal and the volume of the observed hydrogen.

## Results

The tetragonal structure of hafnium dihydride, as reported previously (Sidhu \& McGuire, 1952), is isomorphous with that of zirconium dihydride (Rundle, Shull \& Wollan, 1952a, b; Hägg, 1930). When the axes of the face-centered tetragonal cell are trans-


Fig. 1. Body-centered tetragonal unit cell of $\mathrm{HfH}_{2}$ structure.
formed to body-centered tetragonal, the unit cell (Fig. 1) contains $2 \mathrm{HfH}_{2}$ with:

$$
\begin{aligned}
& \text { Hf: } 0,0,0 ; \frac{1}{2}, \frac{1}{2}, \frac{1}{2} . \\
& \mathrm{H}: 0, \frac{1}{2}, \frac{1}{4} ; 0, \frac{1}{2}, \frac{3}{4} ; \frac{1}{2}, 0, \frac{1}{4} ; \frac{1}{2}, 0, \frac{3}{4} .
\end{aligned}
$$

The positions of hafnium atoms were determined from X-ray powdered patterns, and those of deuterium or hydrogen from neutron diffraction patterns (Fig. 2). The calculated and the observed relative intensities for X-ray and neutron scattering are given in Table 1.


Fig. 2. (a) X-ray diffraction pattern of $\mathrm{HfD}_{2}$ (Co $\mathrm{K} \alpha$ radiation; camera diameter 114.6 mm .).
(b) Low-angle portion of neutron diffraction pattern of $\mathrm{HfD}_{2}$.

Table 1. Calculated and observed $X$-ray and neutron diffraction relative intensities $\left(I / I_{0}\right)$ for $\mathrm{HfD}_{2}$

| $\begin{gathered} h k l \\ \text { (B.-c.t.) } \end{gathered}$ | X-rays |  | Neutrons |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & I \mid I_{0}{ }^{*} \\ & \text { (Cale.) } \end{aligned}$ | $\begin{gathered} I / I_{0} \\ \text { (Obs.) } \end{gathered}$ | $\begin{gathered} I \mid I_{0} \\ \text { (Cale.) } \end{gathered}$ | $\begin{gathered} I \mid I_{0} \\ \text { (Obs.) } \end{gathered}$ |
| 101 | 100.0 | vs | 47.4 | 45 |
| 110 | $37 \cdot 4$ | $s$ | $0 \cdot 6$ | - |
| 002 | $13 \cdot 1$ | $m$ | 0.2 | - |
| 200 | $12 \cdot 8$ | $m$ | 56.0 | 56 |
| 112 | 20.7 | $m+$ | $100 \cdot 0$ | 100 |
| 211 | $29 \cdot 3$ | $s$ | $30 \cdot 2$ | 34 |
| 202 | 11.8 | $m$ | $13 \cdot 6$ | 12 |
| 103 | 11.5 | $m$ |  |  |
| 220 | $4 \cdot 7$ | $\boldsymbol{w}$ |  |  |
| 301 | 8.7 | $m$ - |  |  |
| 310 | 8.7 | $m-$ |  |  |
| 004 | $2 \cdot 2$ | $v w$ |  |  |
| 222 | 8.9 | $w+$ |  |  |
| 213 | 18.3 | $m+$ |  |  |
| 114 | $10 \cdot 7$ | $m$ |  |  |
| 312 | $22 \cdot 8$ | $m+$ |  |  |
| 321 | 15.6 | $m$ |  |  |
| 204 | 20.0 | $m+$ |  |  |
| 303 | $35 \cdot 6$ | $s$ |  |  |

* X-ray diffraction intensities were calculated by using atomic scattering factors of Hf only; neutron diffraction intensities were calculated by using scattering amplitudes of both Hf and D; the intensities were not corrected by temperature factor.

For a cylindrical sample the intensities were calculated from the following equations:

For X-rays, $I \propto|F|^{2} m \frac{1+\cos ^{2} 2 \theta}{\sin ^{2} \theta \cos \theta}$.
For neutrons, $I \propto \frac{|F|{ }^{2} m}{\sin ^{2} \theta \cos \theta}$.

The neutron scattering amplitude for hafnium was calculated from the observed intensities of diffraction peaks and was found to be approximately $+0.97 \times 10^{-12}$ cm . It was based on the scattering amplitude of deuterium as $0.65 \times 10^{-12} \mathrm{~cm}$.

X-ray diffraction patterns of $\mathrm{HfH}_{1.98}$ and $\mathrm{HfH}_{2.10}$, (Fig. 3) show a marked contrast. The interplanar spacings (Table 2) of planes of high $l$ indices, such as

Table 2. Diffraction data for $\mathrm{HfH}_{1.98}$ and $\mathrm{HfH}_{2.10}$

| $\begin{gathered} h k l \\ \text { (B.-c.t.) } \end{gathered}$ | $\mathrm{HfH}_{1.98}$ |  | $\mathrm{HfH}_{2.10}$ |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $d$ (A) | $I / I_{0}$ | $d$ ( $\AA$ ) | $I / I_{0}$ |
| 101 | 2.72 | $v s$ | $2 \cdot 71$ | $v s$ |
| 110 | $2 \cdot 45$ | $s$ | $2 \cdot 46$ | $s$ |
| 002 | 2.199 | $m$ | 2.181 | $m$ |
| 200 | 1.732 | $m$ | 1.737 | $m$ |
| 112 | 1.637 | $m+$ | 1.633 | $s$ |
| 211 | $1 \cdot 460$ | $s$ | $1 \cdot 466$ | $s$ |
| 202 | 1.361 | $m$ | 1.359 | $m$ |
| 103 | $1 \cdot 351$ | $w+$ | 1.344 | m- |
| 220 | 1-223 | $\boldsymbol{w}$ | $1 \cdot 230$ | $w$ |
| 301 | $1 \cdot 116$ | m | 1-121 | $m$ |
| 310 | 1.093 | $m$ - | 1-102 | $m$ - |
| 004 | - | - | 1.691 | $v w$ |
| 222 | 1.069 | vw | 1.072 | $w+$ |
| 213 | 1.065 | m+ | 1.062 | $m$ |
| 114 | 1.004 | $\boldsymbol{w}$ | 0.997 | $w$ |
| 312 | 0.979 | $m+$ | 0.982 | $m$ |
| 321 | 0.937 | $m$ | 0.941 | $m$ |
| 204 | 0.928 | $m$ | 0.924 | $m+$ |
| 303 | 0.906 | , | 0.906 | - |

(002), (103), (004), (204), etc. are considerably decreased and those of high $h k$ indices are generally increased. The structure constants calculated from the diffraction data of the two hydrides and of hafnium metal are given in Table 3.


Fig. 3. X-ray diffraction pattern of hafnium dihydrides (Co $K \alpha$ radiation; camera diameter $114 \cdot 6 \mathrm{~mm}$.).
Table 3. Structure constants of $\mathrm{Hf}, \mathrm{HfH}_{1.98}$ and $\mathrm{HfH}_{2.10}$

| Composition | Structure | Lattice parameters | Interatomic distances ( $\AA$ ) | Volume of unit cell ( $10^{-24} \mathrm{~cm} .^{3}$ ) | Calculated density (g.cm. ${ }^{-3}$ ) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Hf | Hexagonal | $\begin{aligned} a_{0} & =3.198 \pm 0.003 \AA \\ c_{0} & =5.055 \pm 0.003 \AA \\ c_{0} / a_{0} & =1.581 \end{aligned}$ | About Hf: <br> 6 Hf at $3 \cdot 198 \pm 0.003$ <br> 6 Hf at $3.131 \pm 0.003$ | $44 \cdot 77$ | 13.25 |
| $\mathrm{HfH}_{1.98}$ | Tetragonal | $\begin{aligned} a_{0} & =3 \cdot 461 \pm 0.002 \AA \\ c_{0} & =4.395 \pm 0.002 \AA \\ c_{0} / a_{0} & =1.270 \end{aligned}$ | About H: <br> 4 Hf at $2.050 \pm 0.002$ <br> About Hf: <br> 8 H at $2.050 \pm 0.002$ <br> 8 Hf at $3.289 \pm 0.002$ <br> 4 Hf at $3.461 \pm 0.002$ | $52 \cdot 65$ | 11-39 |
| HfH ${ }_{2 \cdot 10}$ | Tetragonal | $\begin{aligned} a_{0} & =3.478 \pm 0.002 \AA \\ c_{0} & =4.361 \pm 0.002 \AA \\ c_{0} / a_{0} & =1.254 \end{aligned}$ | About H: <br> 4 Hf at $2.053 \pm 0.002$ <br> About Hf: <br> 8 H at $2.053 \pm 0.002$ <br> 8 Hf at $3.287 \pm 0.002$ <br> 4 Hf at $3.478 \pm 0.002$ | 52.75 | $11 \cdot 37$ |

## Discussion

In the crystal structure of hafnium metal (Table 3) each atom is surrounded by 12 like atoms, 6 at a distance $3.198 \AA$ and the other 6 at $3.131 \AA$. The metal-metal bonds are essentially of the same length. In the lattice of hafnium dihydride, each metal atom is also surrounded by 12 like atoms, but in this case 8 hafnium atoms are at $3 \cdot 289 \AA$, the distance of nearest approach of metal-metal atoms, and 4 hafnium atoms at $3 \cdot 461 \AA$ or $a_{0}$ in the ( 001 ) plane. These give rise to short and long metal-metal bonds respectively in the $\mathrm{HfH}_{2}$ structure. In addition each metal atom is surrounded by 8 hydrogen atoms that are located in the flattened tetrahedra of metal atoms equidistant from 4 hafnium.

As the unit cell is formed at $\mathrm{HfH}_{1.87}$, all normal sites for hydrogen atoms do not seem to be occupied. Absorption of additional hydrogen in samples prepared by long annealing and slow cooling at sufficient gas pressure forms additional Hf-H bonds. These bonds apparently drain electrons from the metalmetal bonds in the ( 001 ) plane, thus weakening the
latter and causing an increase in $a_{0}$. On the other hand there is general strengthening of the short bonds; they either decrease or remain practically the same in length. As a result there is a further compression of the structure along the $c$ axis, causing a decrease in $c_{0}$. The increase $\Delta a_{0}$ and the decrease $\Delta c_{0}$ are related by the expression: $\Delta a_{0}=\frac{1}{2}\left(c_{0} / a_{0}\right)\left|-\Delta c_{0}\right|$.

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